Aim:To show a double slit interference pattern and the influence of slit-separation.Subjects:6D10 (Interference From Two Sources)Diagram:Image: Image and the influence of slit-separation in the influence of slit-separation in the influence of slit-separation.



- Equipment:
- Steel table.
- Magnetic clamps, used to fix the components to the steel table.
- Laser, 50mW.
- Two surface mirrors (1/10λ).
- Lens, f=+10mm.
- Lens, f=+50mm.
- Adjustable diaphragm (when needed).
- Slide holder.
- Lens, f=132mm.
- Optical rail, I=1m, as guiding ruler.
- Slide with four double slits (Leybold 46985), all slits having a width of .20mm and slit-separation of: a, 1.00mm; b, .75mm; c, .50mm; d, .25mm.
- Overhead sheet with slit dimensions on it.
- Safety:

#### Even relatively small amounts of laser light can lead to permanent eye

**injuries**. The laser we use is a class 3B laser. A Class 3B laser is hazardous if the eye is exposed directly, but diffuse reflections such as from paper or other <u>rough</u> surfaces are not harmful. Protective eyewear is typically required where direct viewing of a class 3B laser beam may occur. In our demonstration we always take measures such that no direct or reflected laser light is directed towards the audience. When needed we use black screens to block such light: all beams are stopped at the edge of the optical table. No watches or other jewelry are carried by the demonstrator. As an extra safety measure is our Class-3B laser equipped with a key switch, so unauthorized people cannot switch the laser on.



### Presentation: Preparation

The demonstration is set up as shown in Diagram:

-The two mirrors are positioned in such a way that the laser beam passes parallel to the table.

-The two lenses (+10mm and +50mm) are positioned at an intermediate distance of 60mm. Having passed these lenses, the laser beam is broadened (and a little divergent). Take care that the broadened beam is still parallel to the table.

-The lens of 132mm can easily be shifted in this beam up and down using the carefully positioned guidance rail.

#### **Demonstration**

The set-up as described in "<u>Preparation</u>" is shortly explained to the students. The most important in this explanation is that the double slit will be placed in a broadened beam and that the double slit will be illuminated by plane waves.

The slide with the double slits is placed on an overhead projector, so the students can see the configuration. The dimensions are indicated on an overhead sheet that is projected at the same time.

The laser is switched on, the broadened beam projects on the wall. When the +132mm lens is placed at the end of the table, this spot is enlarged (see Figure 1A; the diameter of the projected spot is around 1m). Then the double slit is shifted into the beam starting with configuration **a** (see Equipment).



### Figure 1

The typical interference pattern appears (see Figure 1B; Figure 1C shows a snapshot of a real projection on the wall). Then we shift to configuration **b**, then **b** and finally **b**; in that way going from large to smaller slit-separation. It is observed that with smaller slit-separation the distance between the lines of interference increases

**Explanation:** Young explained the observed pattern with the Huygens wave theory and so introduced the principle of interference. Many textbooks give the explanation. Figure 2 shows the arrangement: s is very large compared to the slit separation b.





In P, ray  $r_1$  and ray  $r_2$  interfere. This interference will be constructive when  $r_1$ - $r_2$ =m $\lambda$  (m=0,1,2,3,...).

Also  $y_m \approx \frac{s}{b}m\lambda$ , and the difference in position of two constructive maxima is  $\Delta y \approx \frac{s}{b}\lambda$ , explaining the equidistance between the observed maxima and the influence of b in

explaining the equidistance between the observed maxima and the influence of b in consistency with what we saw in the Presentation. Interference term

#### Remarks:

• A more complete analysis, also including the diffraction of each slit gives for the

intensity (1) at P: 
$$I(\theta) \approx \left[\frac{\sin\left(\frac{\pi a \sin \theta}{\lambda}\right)}{\frac{\pi a \sin \theta}{\lambda}}\right] \times \underbrace{\cos^2\left(\frac{\pi b \sin \theta}{\lambda}\right)}_{\text{Interference term}}$$

If *a* becomes vanishingly small, then the diffraction envelope term approaches 1, and only interference is present. This is the condition for a good Young's double slit experiment. With a=.20mm this appears to work satisfactory. Using double slits with larger a, then next to interference also diffraction becomes visible in our set-up and that is a different demonstration.

- The +132mm lens is positioned at a distance of about 1m away from the slide with the double slit. This means that on the wall an image is projected of a point around 85 cm (1m-132mm) away from the double slit. In that way it is assured that the diffraction envelope is really wide (Fraunhofer diffraction). Closer to the slide, the diffraction envelope will transfer into a Fresnel diffraction pattern, spoiling our demonstration. The transition form Fraunhofer to Fresnel diffraction occurs in this set-up at around (s=a<sup>2</sup>/2 $\lambda$ =) 28cm (see the demonstration "Fraunhofer-Fresneldiffraction" in this database).
- In Young's historical experiment plane waves were obtained using a pinhole through which sunlight passed before illuminating two close-together pinholes. In this way he obtained spatial coherence between the two pinholes. Since we use a laser, the initial pinhole is not needed.
- When in the demonstration the +132mm lens is removed we see that the interference-pattern is enveloped in a wider diffraction-pattern. This can be shown when diffraction has been treated.



Sources:

### • Hecht, Eugene, Optics, pag. 385-388 and 447-451

- Mansfield, M and O'Sullivan, C., Understanding physics, pag. 329-331
- Young, H.D. and Freeman, R.A., University Physics, pag. 1142-1148
- <u>Giancoli, D.G., Physics for scientists and engineers with modern physics</u>, pag. 870-872 and 893-895

