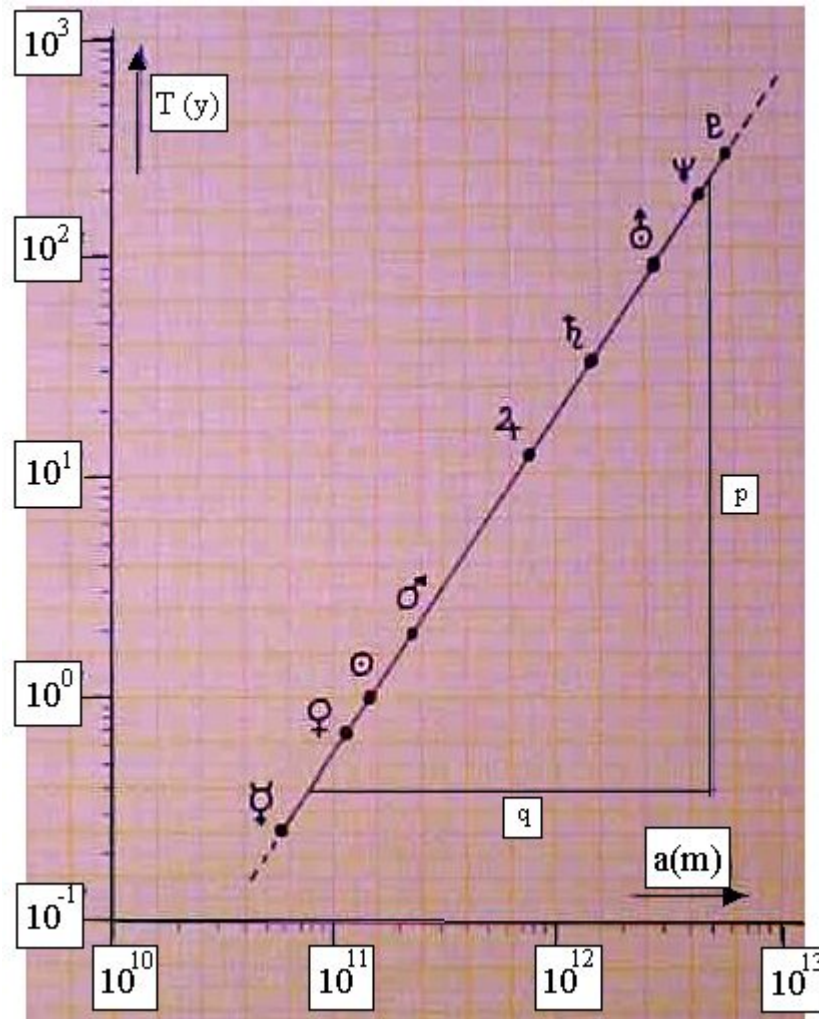


Kepler's third law

Aim: To show empirically that Kepler's third law is true.

Subjects: 1L20 (Orbits)
8A10 (Solar System Mechanics)

Diagram:



- Equipment:**
- Graph on overhead sheet, $T=f(a)$, T and a both scaled logarithmically.
 - Table with data of the planetary system (see Sources).

Kepler's third law

Presentation: The graph is projected by means of an overhead sheet. The relationship with the table of planetary data is elucidated. Clearly can be observed that the data fit on a straight line in such a double logarithmic graph. The slope of this line (p/q) equals 1.5. This is the relationship of the powers in Kepler's third law: $T^2 \propto a^3$.

Explanation: Kepler's third law states $T^2 = \text{const.} \cdot a^3$. Taking logarithms on both sides, we can also write: $2 \log T = \log \text{const.} + 3 \log a$ and: $\log T = \frac{1}{2} \log \text{const.} + \frac{3}{2} \log a$. So when T and a are graphed logarithmically (with x - and y -decades equally spaced), we see a line whose slope ($\frac{3}{2}$) is the power-relationship in the original function.

Simulations: On the internet you can find many simulations that are appropriate. For instance on: www.walter-fendt.de, www.physics.sjsu.edu/Tomley/demos.htm and www.astro.unl.edu/naap/pos/animations/kepler.swf.

Sources:

- [Mansfield, M and O'Sullivan, C., Understanding physics](#), edition 1998, pag. 106-107 and 741 (planetary data).
- [BINAS tabellenboek](#), vijfde druk, tabel 31.
- [McComb, W.D., Dynamics and Relativity](#), edition 1999, pag. 72-74.
- [Roest, R., Inleiding Mechanica](#), vijfde druk, pag. 257-258.
- [Stewart, J, Calculus](#), edition 1999, pag. 867.